Reg. No. : $\qquad$
Name: $\qquad$
II Semester B.A. Degree (CBCSS - OBE - Regular/Supplementary/ Improvement) Examination, April 2023

## (2019 Admission Onwards)

## COMPLEMENTARY ELECTIVE COURSE IN ECONOMICS/DEVELOPMENT ECONOMICS <br> 2C02ECO/DEVECO : Mathematics for Economic Analysis - II

Time: 3 Hours
PART - A
(Answer all questions. Each carries 1 mark)

1. What do you mean by integration?
2. Find $\int x^{-1} d x$ where $x>0$.
3. Define a square matrix.
4. What do you mean by scalar multiplication of matrix ?
5. What is meant by discriminant of a matrix ?
6. Define Eigen value.
PART - B
(Answer any six questions. Each carries 2 marks)
7. Solve $\int\left(5 x^{2}-3 x+1\right) d x$.
8. Distinguish between initial conditions and boundary conditions in the case of indefinite integrals.
9. Given the marginal cost function $M C=25+30 Q-9 Q^{2}$ and fixed cost FC $=55$, find total cost.

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10. Distinguish between identity matrix and null matrix.
11. Explain the commutative, associative and distributive laws in matrix algebra.
12. Given $A=\left[\begin{array}{lll}2 & 3 & 5 \\ 5 & 1 & 2 \\ 2 & 3 & 5\end{array}\right]$, prove that $A$ is a singular matrix.
13. Define the rank of a matrix.
14. What is characteristic matrix ?
PART - C
(Answer any four questions. Each carries 3 marks)
15. Determine the following integral using the substitution method: $\int 10 x\left(x^{2}+3\right)^{4}$.
16. Explain the properties of definite integrals.
17. Explain the properties of determinants.
18. Find the inverse of the matrix $\left[\begin{array}{lll}4 & 2 & 5 \\ 3 & 1 & 8 \\ 9 & 6 & 7\end{array}\right]$.
19. Use discriminants to determine whether the following quadratic function is positive or negative definite $y=-3 x_{1}^{2}+4 x_{1} x_{2}-4 x_{2}^{2}$.
20. Given $A=\left[\begin{array}{cc}-6 & 3 \\ 3 & -6\end{array}\right]$ find the characteristic roots of $A$.

## PART - D

(Answer any two questions. Each carries 5 marks.)
21. Given the demand function $P_{d}=113-Q^{2}$ and the supply function $P_{s}=(Q+1)^{2}$, assuming pure competition, find the consumers' surplus and producers' surplus.
22. Use Cramer's rule to solve for the unknowns in the following :
$5 x_{1}-2 x_{2}+3 x_{3}=16$
$2 x_{1}+3 x_{2}-5 x_{3}=2$
$4 x_{1}-5 x_{2}+6 x_{3}=7$
23. Determine the rank of the matrix $\left[\begin{array}{ccc}-8 & 2 & -6 \\ 10 & -2.5 & 7.5 \\ 24 & -6 & 18\end{array}\right]$.
24. Minimize a firm's total costs $\mathrm{c}=45 \mathrm{x}^{2}+90 \mathrm{xy}+90 \mathrm{y}^{2}$ when the firm has to meet a production quota equal to $2 x+3 y=60$ by finding the critical values and using the bordered Hessian to test the second-order conditions.

