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Reg. No.:

Name :

III Semester B.Sc. Degree (CCSS-Reg./Supple./Imp.)

Examination, November 2014

COMPLEMENTARY COURSE IN MATHEMATICS

3C03 MAT: Differential Equations, Laplace Transforms, Fourier Series and Partial Differential Equations

Time	•	3	H	lo	u	rs

Max. Weightage: 30

- 1. Fill in the blanks:
 - a) Number of arbitrary constants in the solution of a first degree first order ordinary differential equation is _______
 - b) Laplace transform of coshat is _____

 - d) One dimensional heat equation is _____

(Weightage: 1)

Answer any six from the following:

- 2. What do you mean by exact differential equation?
- 3. Solve $\frac{dy}{dx} = \frac{x}{y}$.
- 4. Reduce the differential equation $y' + p(x)y = g(x)y^n$ to linear equation by using suitable substitution.
- 5. What do you mean by a self-orthogonal curve?
- 6. Find Laplace transform of sin32t, and which the contribute with the to accomplish the first sind to the contribute of the contribute of
- 7. State second shifting theorem for Laplace transform.





- 8. Find inverse Laplace transform of $\frac{s}{(s-1)(s-2)}$.
- 9. State half range Fourier Cosine series formula.
- Verify that $u = e^{-t} \sin x$ satisfies one dimensional heat equation by assuming suitable value for the constant in the heat equation. (Weightage: 6×1=6)

Answer any seven from the following:

11. Solve
$$(x + 1) \frac{dy}{dx} - y = e^{3x} (x + 1)^2$$
.

- $\sqrt{2}$. Find the orthogonal trajectories of xy = c.
- 13. Using method of variation of parameters, solve $y'' + y = \tan x$.

14. Solve
$$\frac{dx}{dt} + 2x - 3y = 0$$
; $\frac{dx}{dt} - 3x + 2y = 0$.

- 15. Find the Laplace transform of te-t cos t.
- 16. Find inverse Laplace transform of $\frac{se^{-s/2} + \pi e^{-s}}{s^2 + \pi^2}$
- 17. Find the Laplace transform of the periodic function

$$f(t) = \begin{cases} \sin \omega t & 0 < t < \frac{\pi}{\omega} \\ 0 & \frac{\pi}{\omega} < t < \frac{2\pi}{\omega} \end{cases}, \ f\left(t + \frac{2\pi}{\omega}\right) = f(t).$$

- 18. Find the Fourier sine series of f(x) = x in (0, 2).
 - 19. Find a solution u(x, y) of the partial differential equation $u_{xx} u = 0$.
 - 20. Using the method of separation of variables, solve the PDE $u_{xx} + u_{yy} = 0$.

(Weightage: $7 \times 2 = 14$)



Answer any three from the following:

- 21. Solve the initial value problem $y'' + 2y' + 5y = 1.25e^{0.5x} + 40\cos 4x 55\sin 4x$, y(0) = 0.2, y'(0) = 60.1.
- 22. Using Laplace transform, solve y''' + 2y'' y' 2y = 0, y(0) = 0, y'(0) = 0 and y''(0) = 6.
- 23. Expand f(x) = |x| in Fourier series in the interval $(-\pi, \pi)$. Also deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} \dots = \frac{\pi^2}{8}.$
 - 24. Find the Fourier series of period 21 for the function

$$f(x) = \begin{cases} l - x & 0 \le x \le l \\ 0 & l \le x \le 2l \end{cases}.$$

25. Using the method of separation of variables, obtain the possible solution of one dimensional heat equation. (Weightage: 3×3=9)